

(b) Find all points  $(x, y)$  on the curve where the line tangent to the curve has slope  $\frac{1}{2}$ .

$$\frac{dy}{dx} = \frac{y}{(2y - x)}$$

$$\frac{y}{(2y - x)} = \frac{1}{2}$$

Set the first derivative equal to  $\frac{1}{2}$ .

$$2y = 2y - x$$

Cross multiply

$$x = 0$$

Subtract  $2y$  from both sides

$$y^2 = 2$$

Plug in  $x = 0$  to the original equation:  $y^2 = 2 + xy$ .

$$y = \pm\sqrt{2}$$

Take the square root of both sides, remember both positive and negative solutions.

$$(0, \sqrt{2}), (0, -\sqrt{2})$$

Final solution, remember  $x = 0$ .